

1 Fluctuations in a Fermi gas

(K&K 7.11) Show for a single orbital of a fermion system that

$$\langle(\Delta N)^2\rangle = \langle N\rangle(1 + \langle N\rangle) \quad (1)$$

if $\langle N\rangle$ is the average number of fermions in that orbital. Notice that the fluctuation vanishes for orbitals with energies far enough from the chemical potential μ so that $\langle N\rangle = 1$ or $\langle N\rangle = 0$.