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A fishing net  $S$  is in the shape of a triangular trough, as shown in the picture. The triangular sides are at  $x = 0$  and  $x = 5$ , the rectangular sides are at  $45^\circ$  to the vertical, and the bottom is at  $z = 0$ ; all lengths are measured in cm. There is no netting across the top, which is at  $z = 1$ . Water is draining out of the net; the motion of the water is described by the vector field  $\vec{F} = \rho \left( a e^{\kappa z^2} \hat{y} - b \hat{z} \right)$  where  $a = 3 \frac{\text{cm}}{\text{s}}$ ,  $b = 5 \frac{\text{cm}}{\text{s}}$ ,  $\kappa = 2 \text{ cm}^{-2}$ , and  $\rho$  is the (constant) density of the water in  $\frac{\text{g}}{\text{cm}^3}$ . The goal of this problem is to find the best way to evaluate the flux

$$\iint \vec{F} \cdot d\vec{S}$$

of water *down* through  $S$ .

- Set up the above surface integral, **but do not evaluate it**  
*Your answer should be ready to integrate; among other things, all substitutions should be made, and you should determine the correct limits.*
- **Use the Divergence Theorem** to find another way to do the problem.  
*This time, complete the computation.*