Find the Fourier transform of the (simplified) Gaussian function

$$f(x) = e^{-x^2} \tag{1}$$

You may want to use the value of the following integral

$$\int_{-\infty}^{\infty} e^{-x^2}\, dx = \sqrt{\pi} \tag{2}$$