

### Representations of the Infinite Square Well

Consider three particles of mass  $m$  which are each in an infinite square well potential at  $0 < x < L$ . The energy eigenstates of the infinite square well are:

$$E_n(x) = \sqrt{\frac{2}{L}} \sin\left(\frac{n\pi x}{L}\right)$$

with energies  $E_n = \frac{n^2\pi^2\hbar^2}{2mL^2}$   
The particles are initially in the states, respectively:

$$|\psi_a(0)\rangle = A[2i|E_4\rangle - 3|E_{10}\rangle]$$

$$\psi_b(x, 0) = B\left[i\sqrt{\frac{8}{L}}\sin\left(\frac{4\pi x}{L}\right) - \sqrt{\frac{18}{L}}\sin\left(\frac{10\pi x}{L}\right)\right]$$

$$\psi_c(x, 0) = Cx(x - L)$$

For each particle:

1. Determine the normalization constant.
2. At  $t = 0$  what is the probability of measuring the energy of the particle to be  $\frac{8\pi^2\hbar^2}{mL^2}$ ?
3. Find state of the particle at a later time  $t$ .
4. What is the probability of measuring the energy of the particle to be the same value  $\frac{8\pi^2\hbar^2}{mL^2}$  at a later time  $t$ ?
5. What is the probability of finding the particle to be in the first half of the well?