

1 Shooting a Box

Suppose the spaceship is approaching the Earth at $3c/5$ and shoots a box at a speed of $4c/5$ (from the spaceship's perspective).

- At what velocity will an Earth-bound observer see the box if it is shot directly **towards** the Earth?
- Sensemaking: Reasonable Value*
Briefly discuss why (or why not) your answer seem reasonable.

2 Zapping with d

Zap the following equations with “d”:

- $f = 3x^3 - e^{2x}$
- $g = \sin(y^2)$
- $5z^4 = \ln(p)$

3 Relativistic Explosion

A lump of clay with mass M explodes into two equal pieces m moving directly away from each other.

- What is the speed of each of the pieces after the explosion?
- Sensemaking: Check a Special Case*
Conceptually, what would you expect the speed of the lumps to be if $m = \frac{M}{2}$? Show that your answer to part (a) works for this special case.
- What is the relativistic kinetic energy of each of the pieces?

4 Moving Clocks Run Slow

Imagine that you have a light clock with a period T (1 “tick” takes time T).

Another observer moves relative to you with velocity $+V$

- Draw a spacetime diagram of 1 tick of the your light clock.
- What are the spacetime coordinates of the end of the “tick” of your light clock in:
 - Your reference frame?
 - The other observer's frame?
- Now imagine that the other observer has an identical light clock. Draw a **new** spacetime diagram of 1 “tick” of the other observer's light clock.

- (d) What are the spacetime coordinates of the end of the “tick” of the other observer’s light clock in:
- (a) The other observer’s frame?
 - (b) Your reference frame?
- (e) *Sensemaking: Tell a Conceptual Story*
Imagine that one of your classmates says, “Moving clocks run slow.” Do you agree? Explain your reasoning.

