

1 Zapping with d

Zap the following equations with “d”:

(a) $f = 3x^3 - e^{2x}$

(b) $g = \sin(y^2)$

(c) $5z^4 = \ln(p)$

2 Separable ODEs

Solve the following differential equations by separation. b and c are constants with the appropriate dimensions.

(a) $\frac{dv}{dt} = ct$ where $v(t=0) = v_0$

(b) $\frac{dp}{dm} = -cp$ where $p(m=0) = p_0$

(c) $\frac{dz}{dk} = -b - cz$ where $z(k=0) = z_0$

3 Speed Squared in Curvilinear Coordinates

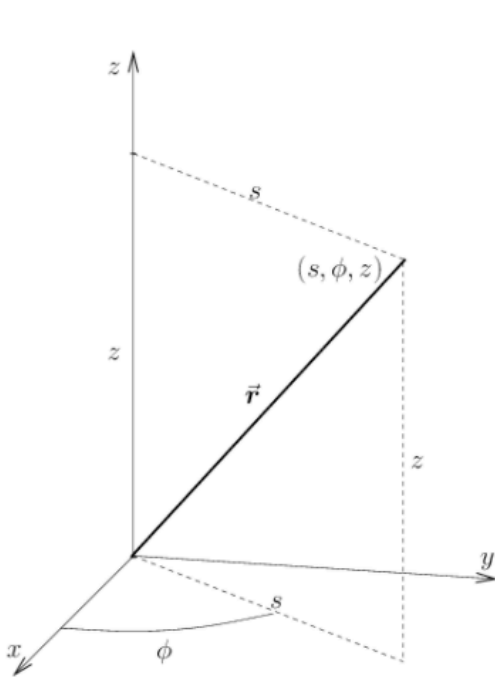
Show that the speed squared written in different standard coordinates systems is:

(a) in rectangular coordinates: $v^2 = \dot{x}^2 + \dot{y}^2 + \dot{z}^2$

(b) in cylindrical coordinates: $v^2 = \dot{s}^2 + s^2\dot{\phi}^2 + \dot{z}^2$

(c) in spherical coordinates: $v^2 = \dot{r}^2 + r^2\dot{\theta}^2 + r^2\sin^2\theta\dot{\phi}^2$

where:

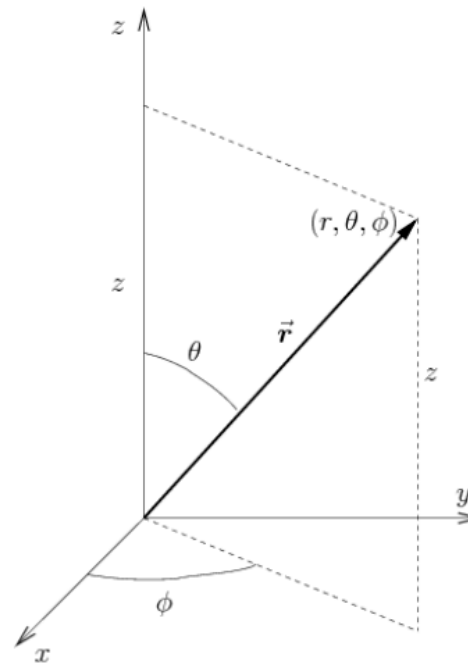


Cylindrical Coordinates

$$x = s \cos \phi$$

$$y = s \sin \phi$$

$$z = z$$



Spherical Coordinates

$$x = r \sin \theta \cos \phi$$

$$y = r \sin \theta \sin \phi$$

$$z = r \cos \theta$$

The algebra for these calculations is a little tedious, but it's good to do them once in your career to convince yourself that these expressions are true!

See: GMM: Curvilinear Coordinates for more discussion of curvilinear coordinates. Note that the labels for the azimuthal and polar coordinates in different for math and physics (ϕ and θ are swapped.)