

1. Let  $x + 3y - z = 2$ .
  - Write down  $d\vec{r}$  for the surface and use what you know to express it in two variables.
  - If one variable is constant, then write down  $d\vec{r}$  in that case. Label this vector  $d\vec{r}_1$ .
  - Describe the vector you obtained above geometrically in relation to the surface.
  - If the other variable is constant, then write down  $d\vec{r}$  in that case. Label this vector  $d\vec{r}_2$ .
  - Compute  $d\vec{r}_1 \times d\vec{r}_2$ . This is  $d\vec{S}$ , the two-dimensional analogue of  $d\vec{r}$ .
  - Is  $d\vec{S}$  tangent to the surface?
2. Consider the surface defined by  $z = 3 - y^2$ .
  - Sketch the surface and describe its normal vector both verbally and graphically.
  - Construct  $d\vec{S}$  as above.
  - Do you think  $d\vec{S}$  is normal to the surface?
3. Let  $M$  be the surface defined by  $x^2 + y^2 = 3$  where  $1 \leq z \leq 3$ .
  - Sketch  $M$ . It includes the ends.
  - Construct  $d\vec{S}$  for  $M$ .
  - Include  $d\vec{S}$  in your sketch.