

1. Let  $\Phi$  be the surface consisting of  $z = 3 - y^2$  above the  $xy$ -plane and the bounded portion of the  $xy$ -plane where  $-2 \leq x \leq 2$  and  $-\sqrt{3} \leq y \leq \sqrt{3}$ .
  - Set-up (an) integral(s) that determines the flux of  $-x\hat{\mathbf{x}} - y\hat{\mathbf{z}}$  through  $\Phi$ .
  - Draw a picture depicting how one could employ the divergence theorem to compute the flux.
  - Carry out the calculation displayed by the picture.
2. Let  $S$  be the sphere of radius 2 inches.
  - Construct a surface integral that represents the flux of  $-x\hat{\mathbf{x}} - y\hat{\mathbf{y}} - z\hat{\mathbf{z}}$  through  $S$ .
  - Construct a triple integral that is equivalent to the flux integral you constructed.
  - Which is easier to compute?
3. Consider the cylinder  $\Sigma$  defined by  $y^2 + z^2 = 5$  and  $2 \leq x \leq 5$  excluding the ends.
  - Construct a surface integral representing the flux of  $x\hat{\mathbf{x}} - (y^2 + z^2)y\hat{\mathbf{y}} - (y^2 + z^2)z\hat{\mathbf{z}}$  through  $\Sigma$ .
  - Use the Divergence Theorem to convert the surface integral into a triple integral.
  - Use a diagram to indicate your method of applying the Divergence Theorem.
  - Compute one of the integrals you've constructed.