

You will probably be doing this activity in-class, from directions given by the instructor. If you are doing it on your own, then choose a point in the room that you are in to be the origin. Imagine that your right shoulder is a point in space, relative to that origin. Point your right arm in succession in each of the directions of the basis vectors adapted the various coordinate systems:

- $\{\hat{x}, \hat{y}, \hat{z}\}$  in rectangular coordinates.
- $\{\hat{s}, \hat{\phi}, \hat{z}\}$  in cylindrical coordinates.
- $\{\hat{r}, \hat{\theta}, \hat{\phi}\}$  in spherical coordinates.

**Solution** The basis vectors for a single coordinate:

- point in the direction in which that coordinate is INCREASING;
- are unit vectors (i.e. STRAIGHT arrows of unit length), even when they are associated with a coordinate which is an angle;
- for curvilinear coordinates (NOT rectangular coordinates), they point in different directions at different points in space;
- provide a nice example of a vector field.

The basis vectors for multiple coordinates in a single orthogonal coordinate system:

- are orthogonal (perpendicular) to each other at each single point;
- can be used to expand any vector at a given point.

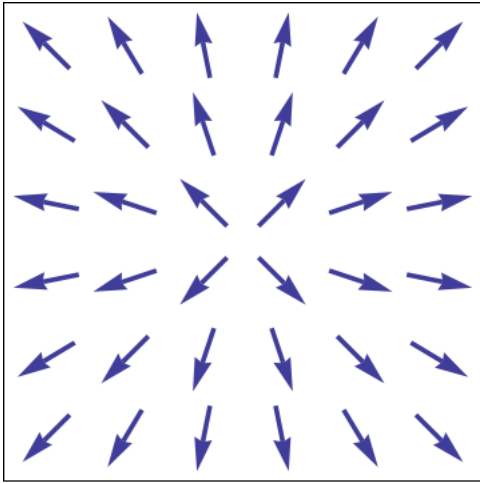


Figure 1: Figure 3: A cross section of the cylindrical coordinate basis vectors  $\hat{s}$  in a plane  $z = \text{constant}$ , as seen from above. Notice that the basis vectors are different from point to point in space.